Prof. Dr. Hendrik Godbersen

Workshop

Statistics & R

| 1 Installation of R, R Studio & Relevant Packages | 6 Inferential Statistics | | |
|---|----------------------------------|--|--|
| 2 Structure of R Studio | 6.1 Principle & Overview | | |
| 3 R Commands | 6.2 Chi-squared Test | | |
| 4 Exercise Data | 6.3 t-test | | |
| 5 Descriptive Statistics | 6.4 ANOVA | | |
| 5.1 Scale of Measurement | 6.5 Shapiro-Wilk Test | | |
| 5.2 Frequencies | 6.6 Wilcoxon Test | | |
| 5.3 Measures of Central Tendency & Dispersion | 6.7 Correlation | | |
| | 6.8 Regression | | |
| | 6.9 Principal Component Analysis | | |
| | | | |

Installation of R, R Studio & Relevant Packages

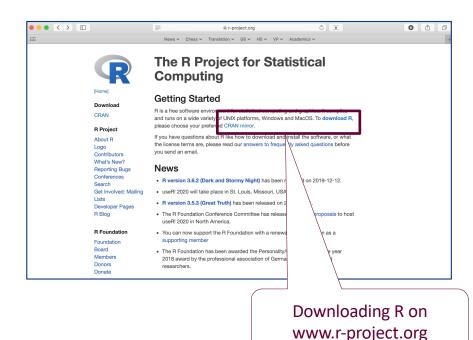
1) Downloading & Installing R

- 1) Go to: https://www.r-project.org/
- 2) Choose a for downloading R
 - > Beware that R matches your system
- 3) Download R
- 4) Install R on your computer

2) Download & Installation von R Studio

- 1) Go to: https://posit.co/download/rstudio-desktop/
- 2) Download R Studio
- 3) Install R Studio on your computer

3) Installing additional R packages

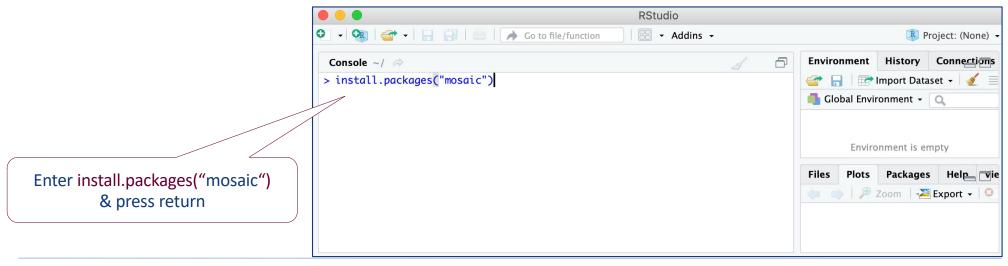


Installation of R, R Studio & Relevant Packages

- 1) Downloading & Installing R ✓
- 2) Download & Installation von R Studio ✓
- 3) Installing additional R packages
 - 1) Make sure that your computer is connected to the internet
 - 2) Enter install.packages("mosaic") in Console
 - 3) Press the return button on your keyboard
 - 4) Repeat this process for all of the required packages

Required R packages:

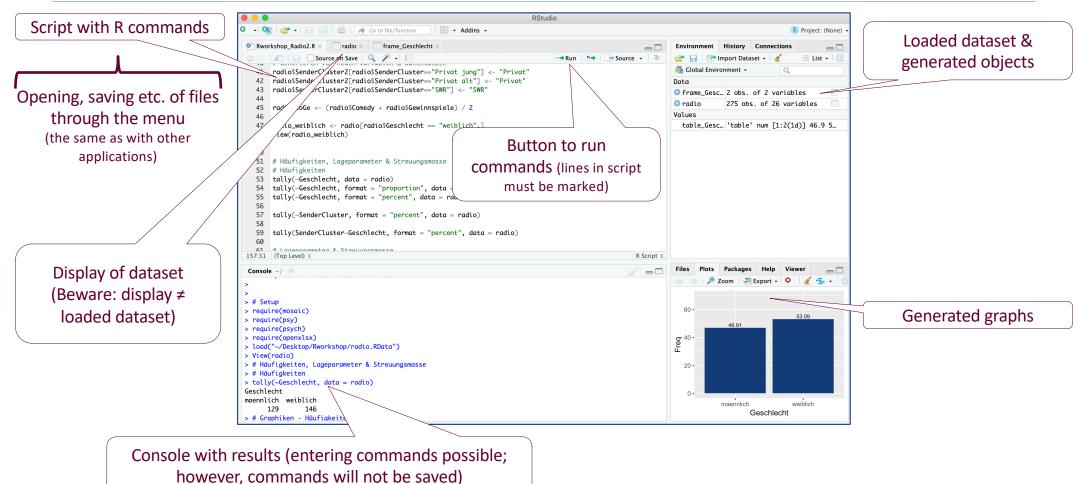
- mosaic
- psy
- psych



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Structure of RStudio

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| | | | |

• Page 1:

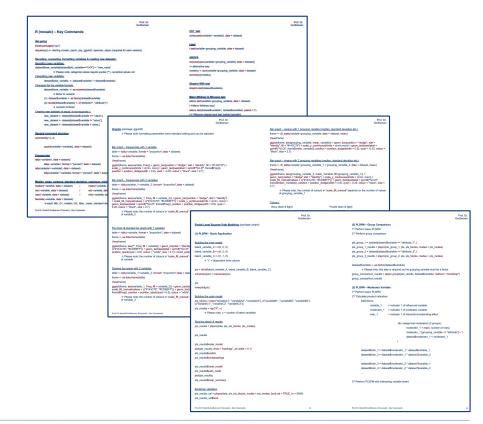
• All commands required for analysing a "normal" research project

• Page 2:

• Generating graphs & exporting results to Excel

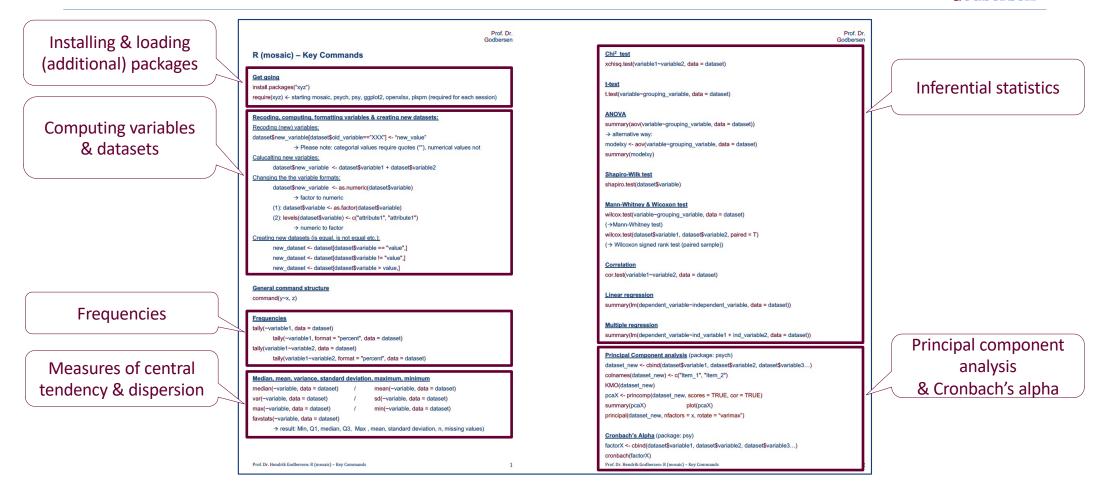
• Page 3:

 PLSPM (partial least squares path modelling) – exceeding standard analyses & not relevant in this course



R Commands: Page 1

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R Commands: Command Structure

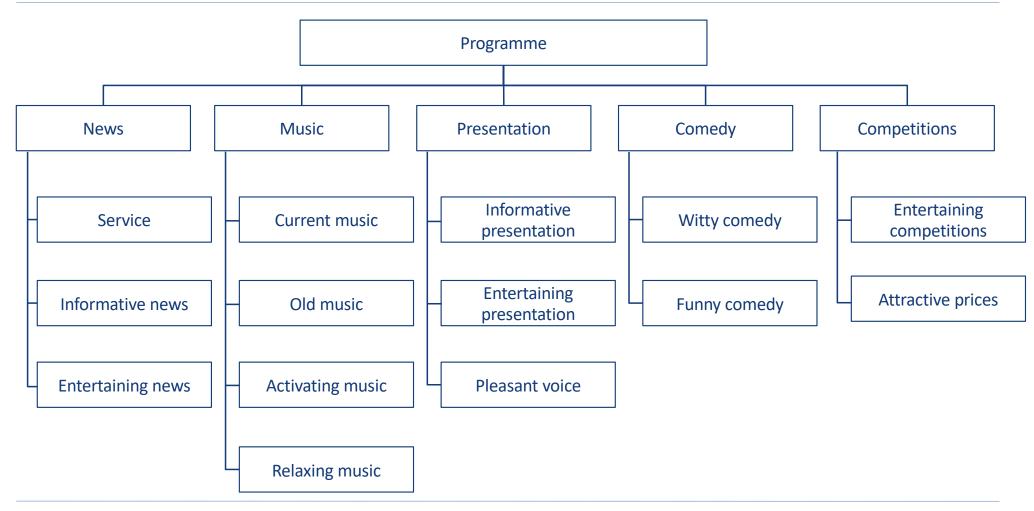
```
General command structure
R (mosaic) - Key Commands
                                                              command(y~x, z)
Get going
install.packages("xyz")
require(xyz) ← starting mosaic, psych, psy, ggplot2, openxlsx, plspm (required for each
Recoding, computing, formatting variables & creating new datasets:
                                                              Frequencies
Recoding (new) variables:
dataset$new_variable[dataset$old_variable=="XXX"] <- "new_value"
          → Please note: categorial values require quotes (***), numerical values
                                                              tally(~variable1, data = dataset)
Calucalting new variables:
     dataset$new variable <- dataset$variable1 + dataset$variable2
Changing the the variable formats:
                                                                            tally(~variable1, format = "percent", data = dataset)
      dataset$new_variable <- as.numeric(dataset$variable)
          → factor to numeric
     (1): dataset$variable <- as.factor(dataset$variable)
                                                             tally(variable1~variable2, data = dataset)
     (2): levels(dataset$variable) <- c("attribute1", "attribute1")
Creating new datasets (is equal, is not equal etc.):
                                                                            tally(variable1~variable2, format = "percent", data = dataset)
     new_dataset <- dataset[dataset$variable == "value",]
     new_dataset <- dataset[dataset$variable != "value".
     new_dataset <- dataset[dataset$variable > value,]
General command structure
                                                                                                             Please note:
                                                                                              Linear regress
command(y~x, z)
                                                                                              summary(lm(de
Frequencies
                                                                                                                           R command (must not be changed)
                                                                                                             red
                                                                                              Multiple regress
tally(~variable1, data = dataset)
                                                                                              summary(Im(de
     tally(~variable1, format = "percent", data = dataset)
tally(variable1~variable2, data = dataset)
                                                                                                                           names of variables or dataset, which must be individually
                                                                                              Principal Comp
     tally(variable1~variable2_format = "percent"_data = dataset)
                                                                                              dataset_new <-
                                                                                                                           adjusted
Median, mean, variance, standard deviation, maximum, minimum
                                                                                              KMO(dataset ne
median(~variable, data = dataset) /
                                                                                              ncaX <- princom
var(~variable, data = dataset)
                        / sd(~variable, data = dataset)
                                                                                                                           dependent variable
                                                                                              summary(pcaX)
                         / min(~variable, data = dataset)
max(~variable, data = dataset)
                                                                                              principal(datase
favstats(~variable, data = dataset)
     → result: Min, Q1, median, Q3, Max, mean, standard deviation, n, missing values)
                                                                                                                           independent variable
                                                                                              factorX <- cbind(
                                                                                              cronbach(factor)
Prof. Dr. Hendrik Godbersen: R (mosaic) - Key Commands
                                                                                              Prof. Dr. Hendrik Go
                                                                                                                           dataset
```

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| | 6.9 Principal Component Analysis |
| | |

Exercise Data: Hypothesised Model



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Exercise Data: Questionnaire & Variables

- station
 - Measurement: main station in the last 2 weeks
- station_cluster
 - Measurement: calculated variable with three attributes
 - Attributes: SWR / private young / private old
- Programme attributes
 - Measurement: Continuous Rating Scale 0 (not good) to 100 (very good)
 - 14 items
 - service
 - informative news
 - entertaining news
 - current music
 - old music
 - activating music
 - relaxing music

- informative presentation
- entertaining presentation
- pleasant voice
- witty comedy
- funny comedy
- entertaining competitions
- attractive prices

- Programme elements
 - Measurement: Continuous Rating Scale -0 (not good) to 100 (very good)
 - 5 items
 - news
 - music
 - presentation
 - comedy
 - competitions
- programme
 - Measurement: Continuous Rating Scale -0 (not good) to 100 (very good)
- gender
 - Measurement: single choice question
- age
 - Measurement: open question
- age_groups (old vs. young, 2 groups)
- current music A (affinity, 2 groups)

Please note: Variable names in red

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Inhalt

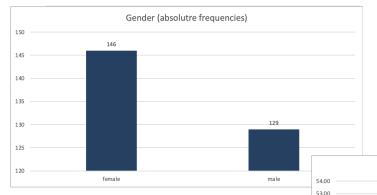
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| | | | |

Scale of Measurement

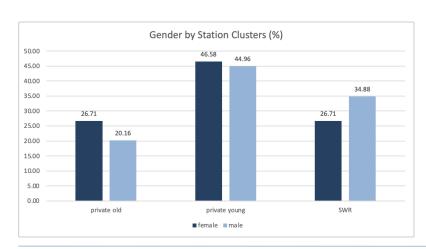
| Scale of measurement | | Mathematical characteristics | Characteristics of values | Example | Measure of central tendency |
|---|----------|------------------------------|--|---------------|---------------------------------------|
| Nominal =/≠ Values are equal or not. Categorical | | Values are equal or not. | Gender | • Mode | |
| (dichotomous) | | | Values are larger, smaller or equal. | Olympic ranks | ModeMedian |
| Metric | Interval | =/≠;;-;+ | The distance between values can be determined. | Temperature | ModeMedian |
| (continuous) | Ratio | =/≠;;+/-; */÷ | The distance and ratio between values can be determined. | Height | Arithmetic mean |

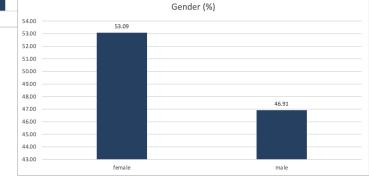
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| | | | |

- Absolute frequency:
 - Number of times a value of a variable occurred



- Relative frequency:
 - Ratio of an absolute frequency of a value to the total number of values for a variable



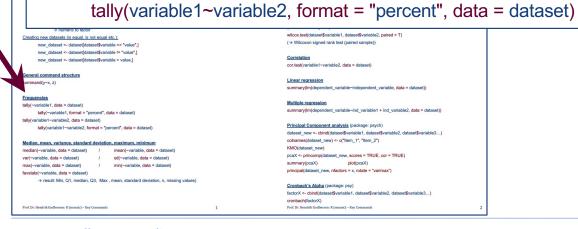


- Cross tabulation (contingency table):
 - Combination of the distribution of two variables

Exercise:

- Of how many men and women does the sample consist?
- What is the proportion of men and women (%)?
- What is the proportion of station clusters (%)?

tally(~variable1, data = dataset) tally(~variable1, format = "percent", data = dataset) tally(variable1~variable2, data = dataset)



| • | station | | Variables |
|---|--|---|--|
| • | station_cluster | | |
| | service informative_news entertaining_news current_music old_music activating_music relaxing_music informative_presentation entertaining_presentation pleasant_voice witty_comedy funny_comedy entertaining_competitions | • | news music presentation comedy competitions programme gender |
| • | attractive_prices | • | age |
| | | • | age_groups current_ music_A |

Variables

Frequencies: Exercise & R Commands (2)

Exercise:

tally(~variable1, format = "percent", data = dataset tally(variable1~variable2, data = dataset)

tally(variable1~variable2, format = "percent", data = dataset)

→ result: Min. Q1, median, Q3, Max, mean, standard deviation, n, missing values

 Median. mean, variance, standard deviation, maximum, minimum

 median(-variable, data = dataset)
 /
 mean(-variable, data = dataset)

 var(-variable, data = dataset)
 /
 sd(-variable, data = dataset)

 max(-variable, data = dataset)
 /
 min(-variable, data = dataset)

favstats/~variable_data = dataset)

Prof. Dr. Hendrik Godbersen: R (mosaic) - Key Commands

• How are men and women distributed over the station clusters (%)?

Frequencies tally(~variable1, data = dataset) tally(~variable1, format = "percent", data = dataset) tally(variable1~variable2, data = dataset) tally(variable1~variable2, data = dataset) tally(variable1~variable2, format = "percent", data = dataset) **Tormatic to tactor* **Creation (new datasets (is equal is not equal dec.): **Torm, dataset - dataset[dataset/variable = "value"] **Tormatic command structure **Torma

Principal Component analysis (package: psych)

colnames(dataset new) <- c("Item 1", "Item 2")

principal(dataset_new.nfactors = x, rotate = "varimax")

Cronbach's Alpha (package: psy)

dataset_new <- chind(dataset\$variable1, dataset\$variable2, dataset\$variable3...)

factorX <- cbind(dataset\$variable1, dataset\$variable2, dataset\$variable3...)

| | Station | | variables |
|---|---------------------------|---|------------------|
| • | station_cluster | | |
| | | | |
| • | service | | |
| • | informative_news | | |
| • | entertaining_news | | |
| • | current_music | | |
| • | old_music | • | news |
| • | activating_music | • | music |
| • | relaxing_music | • | presentation |
| • | informative_presentation | • | comedy |
| • | entertaining_presentation | • | competitions |
| • | pleasant_voice | | |
| • | witty_comedy | • | programme |
| • | funny_comedy | | _ |
| • | entertaining_competitions | • | gender |
| • | attractive_prices | • | age |
| | | | |
| | | • | age_groups |
| | | • | current_ music_A |
| | | | |

station

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Measures of central tendency:

- Arithmetic mean:
 - Sum of all values divided by the number of all values; metric measurement level required
- Median:
 - Value that separates the higher and lower half of a distribution; ordinal measurement level required
- Mode:
 - Most frequent value of frequency distribution; nominal measurement level required

Measures of dispersion:

- Variance
 - Average squared difference of values from their arithmetic mean (please note: empirical variance → /n; sample variance → /n-1)

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

- Standard deviation
 - Average difference of values from their arithmetic mean

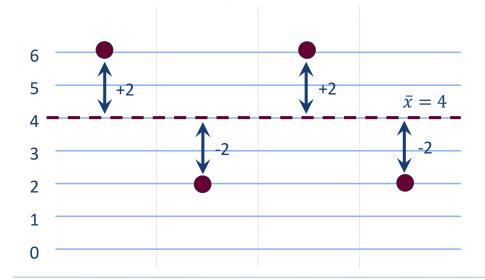
$$\sigma = \sqrt{\sigma^2}$$

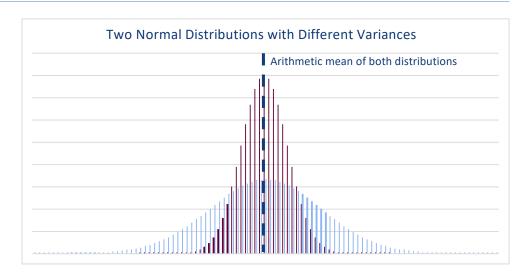
Measures of Central Tendency & Dispersion: Brief

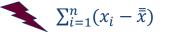
Measures of dispersion

- Variance $\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$
- Standard deviation

$$\sigma = \sqrt{\sigma^2}$$







$$- \left\{ (+2) + (-2) + (+2) + (-2) = 0 \right\}$$

$$\sum_{i=1}^n (x_i - \bar{\bar{x}})^2$$

$$\sum_{i=1}^{n} (x_i - \bar{x})^2 \qquad \begin{cases} (+2)^2 + (-2)^2 + (+2)^2 + (-2)^2 = \\ 4 + 4 + 4 + 4 = 16 \end{cases}$$

$$\sigma^2 = \frac{\sum_{i=1}^{n} (x_i - \bar{x})^2}{n} \qquad \begin{cases} 16/4 = 4 \end{cases}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$\sigma = \sqrt{\sigma^2}$$

$$\sqrt{4} = 2$$

Measures of Central Tendency & Dispersion: Exercise & R Commands (1)

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age_groups

current music A

Exercise:

- What is the average age of the participants (arithmetic mean)?
- What is the median age of the participants?
- What is the variance and standard deviation of the age?



Median, mean, variance, standard deviation, maximum, minimum

median(~variable, data = dataset) / mean(~variable, data = dataset)

var(~variable, data = dataset) / sd(~variable, data = dataset)

max(~variable, data = dataset) / min(~variable, data = dataset)

favstats(~variable, data = dataset)



| • | station station_cluster | | Variables |
|---|--|---|--|
| • | service informative_news entertaining_news current_music old_music activating_music relaxing_music informative_presentation entertaining_presentation pleasant_voice witty_comedy funny_comedy entertaining_competitions attractive_prices | • | news music presentation comedy competitions programme gender age |

Measures of Central Tendency & Dispersion: Exercise & R Commands (2)

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age groups

current music A

Exercise:

- What is the average programme evaluation of the participants (arithmetic mean)?
- What is the median programme evaluation of the participants?
- What is the variance and standard deviation of the programme evaluation?

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Median, mean, variance, standard deviation, maximum, minimum median(~variable, data = dataset) / mean(~variable, data = dataset)

var(~variable, data = dataset) / sd(~variable, data = dataset)

max(~variable, data = dataset) / min(~variable, data = dataset)

favstats(~variable, data = dataset)



station **Variables** station cluster service informative news entertaining news current music news old music music activating music presentation relaxing music comedy informative presentation competitions entertaining presentation pleasant voice programme witty comedy funny comedy gender entertaining competitions age attractive prices

age groups

current music A

Exercise:

- Determine arithmetic mean, median and standard deviation for age with only one R command.
- Determine arithmetic mean, median and standard deviation for programme with only one R command.



Median, mean, variance, standard deviation, maximum, minimum median(~variable, data = dataset) / mean(~variable, data = dataset) var(~variable, data = dataset) / sd(~variable, data = dataset)

max(~variable, data = dataset) / min(~variable, data = dataset)

favstats(~variable, data = dataset)



Variables station station cluster service informative news entertaining news current music news old music music activating music presentation relaxing music comedy informative presentation competitions entertaining presentation pleasant voice programme witty comedy funny comedy gender entertaining competitions age attractive prices

Measures of Central Tendency & Dispersion: Exercise & R Commands (4)

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current music A

Exercise:

- Compare the average age of men and women (arithmetic means).
- Compare the average programme evaluation of men and women (arithmetic means).



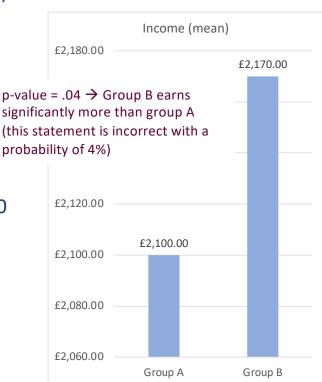
Median, mean, variance, standard deviation, maximum, minimum median(~variable, data = dataset) / mean(~variable, data = dataset) var(~variable, data = dataset) / sd(~variable, data = dataset) max(~variable, data = dataset) / min(~variable, data = dataset) favstats(~variable, data = dataset)



| • | station station_cluster | | Variables |
|---|--|---|--|
| • | service informative_news entertaining_news current_music old_music activating_music relaxing_music informative_presentation entertaining_presentation pleasant_voice witty_comedy funny_comedy entertaining_competitions attractive_prices | • | news music presentation comedy competitions programme gender age |
| | | • | age_groups |

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| | |

- Inferential statistics determines if effects are significant
 - Significant = not coincidental (common language: an effect "really" exists)
 - Non-significant = coincidental (common language: there is no effect)
- The quantitative "black and white world:
 - H1: Effect XY exists.
 - H0: Effect XY does not exist.
- "Logic" of inferential statistical procedures
 - The inferential statistical procedures try to reject H0.
 - The results is the p-value with values between 0 and 1.
 - The p-value indicates the probability that H0 holds true if though H0 was rejected.
- Steps of the analysis
 - (1) p-value → Significance: p < .05 = significant (higher degrees of significance at p < .01 and p < .001
 - (2) If p-value < .05: interpreting the measured values (arith. mean, frequencies etc.) → direction & strength of the effect



Inferential Statistics: Overview

| | Scale of measurement | | Mathematical characteristics | Characteristics of values | Example | Measure of central tendency |
|---|----------------------|----------|------------------------------|--|---------------|-----------------------------|
| | Categorical | Nominal | =/≠ | Values are equal or not. | Gender | • Mode |
| | (dichotomous) | Ordinal | =/≠; | Values are larger, smaller or equal. | Olympic ranks | Mode Median |
| ** Metric (continuous | Metric | Interval | =/≠ ; ; −; + | The distance between values can be determined. | Temperature | Mode Median |
| | (continuous) | Ratio | =/≠;;+/-; */÷ | The distance and ratio between values can be determined. | Height | Arithmetic mean |
| Exploratory Data Analysis • Cluster analysis | | | | | | |

Inferential Statistics: Overview

| Inferential Statistical Procedures | | Independent variable | | |
|------------------------------------|-------------|--|---|--|
| | | categorical (dichotomous) | Metric (continuous) | |
| Dependent | categorical | Chi ² test | Discriminant analysis | |
| variable | metric | t-test*** (2 groups) & Analysis of variances (≥ 3 groups) | Regression (dependence) & correlation (interdependence) | |

*** "Additional" tests:

- Shapiro-Wilk test (tests if a variable is normally distributed; precondition for t-tests at small sample sizes, n ≤ 50)
- Mann-Whitney test/Wilcoxon test (tests if 2 groups differ on an at least ordinally scaled variable, without requiring a normal distribution)

Exploratory Data Analysis

- Principal component analysis
- Cluster analysis

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Chi-squared Test: Brief

Application:

Testing the (in)dependence of two categorical (nominal) variables

Leading question:

• Is there an association of two variables with a nominal measurement level? / Are two categorical variables independent from each other?

Steps of the analysis:

- 1) Is the p-value < .05 (< .01, < .001)? \rightarrow Significance?
- 2) How do the frequencies compare?
- Statistical Analysis ("in the background"):
 - Calculation of the expected frequencies (e) which would indicate no difference between the variables (column sum * row sum / number of observations)
 - 2) Test if the observed values (h) significantly deviate from the expected values €

| | Female | Male | Sum |
|------|------------------|------------------|-----|
| Blue | h = 35 e = 25 | h = 15 e = 25 | 50 |
| Red | h = 15 e = 25 | h = 35 e = 25 | 50 |
| Sum | 50 | 50 | 100 |

- Statistical Analysis ("in the background"):
 - Calculation of the expected frequencies (e) which would indicate no difference between the variables (column sum * row sum / number of observations)
 - 2) Test if the observed values (h) significantly deviate from the expected values €

| V1 | Female | Male | Sum |
|------|------------------|------------------|-----|
| Blue | h = 15 e = 25 | h = 35 e = 25 | 50 |
| Red | h = 35 e = 25 | h = 15 e = 25 | 50 |
| Sum | 50 | 50 | 100 |

$$p$$
-value = 0.0001447

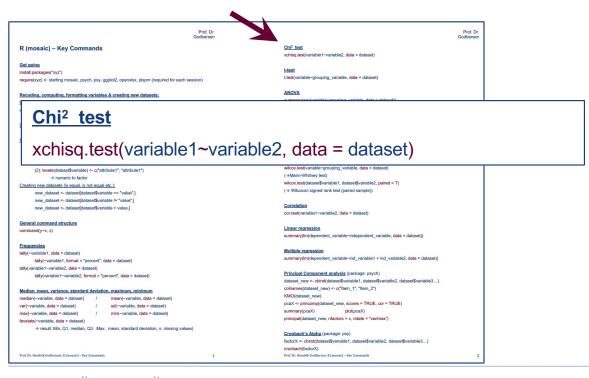
| V2 | Female | Male | Sum |
|------|------------------|------------------|-----|
| Bleu | h = 24 e = 25 | h = 26 e = 25 | 50 |
| Red | h = 26 e = 25 | h = 24 e = 25 | 50 |
| Sum | 50 | 50 | 100 |

p-value = 0.8415

Chi-squared Test: Exercise & R Commands

Exercise:

- Do men and women differ in their preferences for station clusters?
- Do the old and young age segment differ in their affinity to current music? If so, how does this difference look like?



| • | station | | Variables |
|---|---|---|--|
| • | station_cluster | | |
| • | service informative_news | | |
| • | entertaining_news | | |
| | current_music old_music activating_music relaxing_music informative_presentation entertaining_presentation pleasant_voice witty_comedy funny_comedy entertaining_competitions | • | news music presentation comedy competitions programme gender |
| • | attractive_prices | • | age |
| | | • | age_groups current_ music_A |

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t-Test: Brief

Application:

Testing if a metric variable differs between two groups (independent sample t-test)

Leading question:

- Do two groups (samples) differ in a metric variable?
- Does a categorical variable (two groups) effect a metric variable?

Types of t-tests:

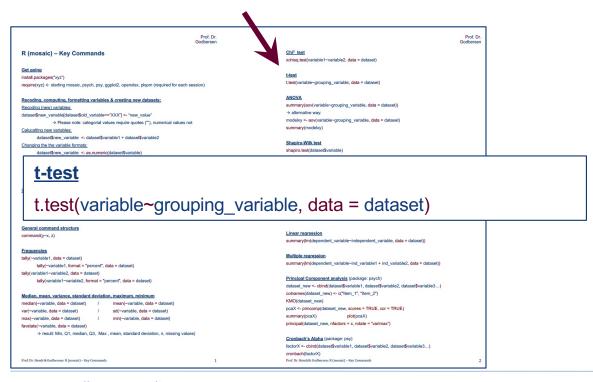
- Independent sample t-test measurements from two groups
- Paired sample t-test two measurement in one group (e.g., before and after)
- One-sample t-test comparison of a group's arithmetic mean with a fixed value

Steps of the analysis:

- 1) Is the p-value < .05 (< .01, < .001)? \rightarrow Significance?
- 2) How do the arithmetic means compare?

Exercise:

- Do men and women evaluate the programme of radio stations differently?
- Do men and women evaluate the music of radio stations differently?



| • | station | | Variables |
|---|---|---|--|
| • | station_cluster | | |
| • | service | | |
| • | informative_news | | |
| • | entertaining_news | | |
| | current_music old_music activating_music relaxing_music informative_presentation entertaining_presentation pleasant_voice witty_comedy funny_comedy | • | news music presentation comedy competitions programme |
| • | entertaining_competitions | • | gender |
| • | attractive_prices | • | age |
| | · | • | age_groups current_ music_A |

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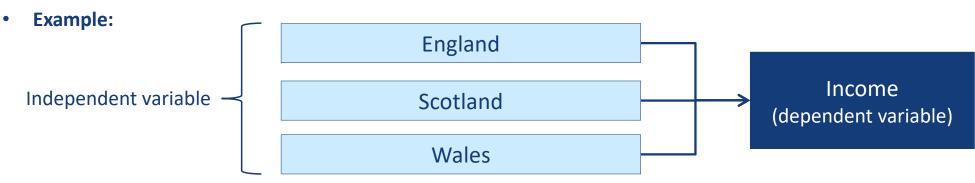
• The ANOVA (analysis of variances) tests if the arithmetic means of three or more groups (samples) systematically differ.

Leading question:

• Do the arithmetic means of three or more groups (samples) differ in a metric variable?

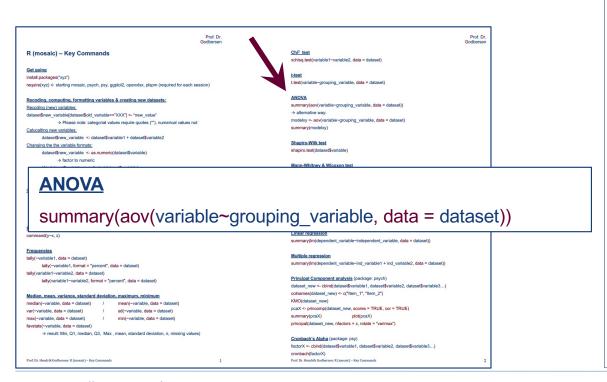
Distinction from t-test:

 Whilst the t-test examines only two groups (samples), the ANOVA analyses three or more groups (samples)



Exercise:

- Do the listeners of the different station clusters evaluate the programme of radio stations differently?
- Do the listeners of the different station clusters evaluate the presentation of radio stations differently?

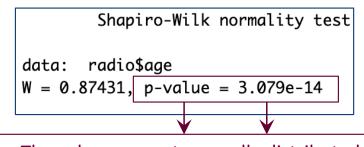


| • | station | | Variables |
|---|--|---|--|
| • | station_cluster | | |
| | service informative_news entertaining_news current_music old_music activating_music relaxing_music informative_presentation entertaining_presentation pleasant_voice witty_comedy funny_comedy entertaining_competitions attractive_prices | • | news music presentation comedy competitions programme gender age |
| | | • | age_groups current_ music_A |

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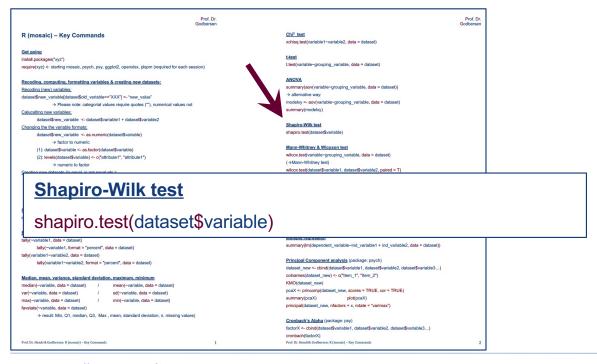
- The Shapiro-Wilk tests <u>compares</u> the <u>values of a variable</u> with <u>normally distributed values</u> to determine if the variable is normally distributed.
- Please note: A normal distribution is a precondition for the application of a t-test if the sample is small (approx. n ≤ 50).
- Leading question & results:
 - Are the values of a metric variable normally distributed?
 - If p ≥ .10 (not significant), the distribution does not differ from a normal distribution → Normal distribution
 - If $p \le .10$ (significant), the distribution differs from a normal distribution \rightarrow no normal distribution
- Consequence of lack of normal distribution:
 - Instead of the t-test, Wilcoxon or Mann-Whitney test is applied (small samples)
 - Please note: It normally makes sense to not only conduct a Shapiro-Wilk test but also graphically examine the distribution



The values are not normally distributed.

Exercise:

- Is the variable age normally distributed?
- Is the variable programme normally distributed?



| • | station | | Variables |
|---|--|---|---|
| • | station_cluster | | |
| • | service informative_news entertaining_news current_music old_music activating_music relaxing_music informative_presentation entertaining_presentation pleasant_voice witty_comedy funny_comedy entertaining_competitions attractive_prices | • | news music presentation comedy competitions programme gender age |
| | | • | age_groups current_ music_A |

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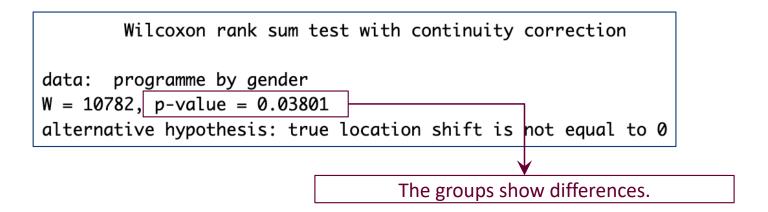
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| | 6.9 Principal Component Analysis | | |
| | | | |

• The Wilcoxon test is a non-parametric procedure that compares the ranks of a variable between two groups (a normal distribution is not required)

• Leading question:

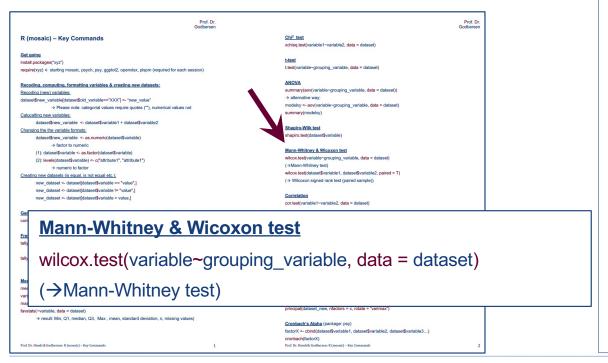
Do two groups differ with regard to a variable on an at least ordinal scale of measurement?

• Example:



Exercise:

- According to the Wilcoxon test, do men and women evaluate the programme of radio stations differently?
- According to the Wilcoxon test, do men and women evaluate the music of radio stations differently?



| • | station | | Variables |
|---|---|---|---|
| • | station_cluster | | |
| • | service informative_news entertaining_news current_music old_music activating_music relaxing_music informative_presentation | | news music presentation comedy competitions |
| • | entertaining_presentation pleasant_voice witty_comedy funny_comedy entertaining_competitions attractive_prices | | programme gender age age_groups |
| | | • | current_ music_A |

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| | |

• A correlation analysis determines the linear association of two metric variables.

Leading question:

- How strong and in what direction is the linear association of two metric variables?
 - → Does the value of variable A increase or decrease if the value of variable B increases or decreases (et vice versa)?

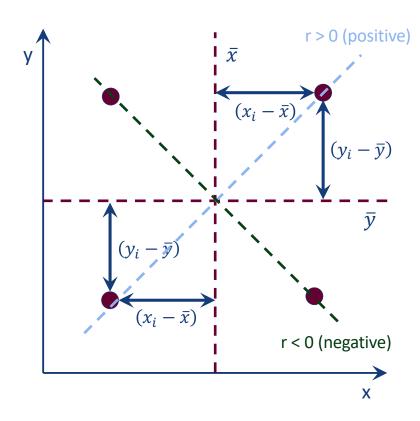
Steps of the analysis:

- 1) Is the p-value < .05 (< .01, < .001)? \rightarrow Significance?
- 2) Which value does the correlation coefficient have?
- Possible interpretation of the correlation coefficient:

| 0 < r ≤ +1.0 | Correlation in the same direction | |
|--------------|---------------------------------------|--|
| -1.0 ≥ r < 0 | Correlation in the opposite direction | |

| 0.0 < r ≤ 0.2 | weak to no correlation |
|-----------------|-------------------------|
| 0.2 < r ≤ 0.4 | weak correlation |
| 0.4 < r ≤ 0.6 | moderate correlation |
| 0.6 < r ≤ 0.8 | strong correlation |
| 0.8 < r ≤ 1.0 | very strong correlation |

Statistical explanation of the correlation coefficient



Covariance (shared dispersion of two variables):

$$cov = \frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})$$

Variance (dispersion of a variable):

$$var = \sigma_x = \frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})^2$$

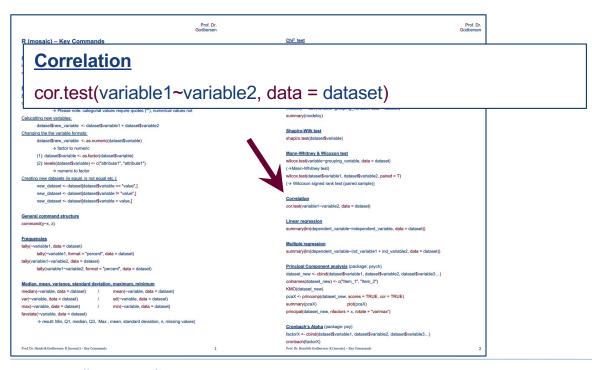
Correlation coefficient (ratio of the shared dispersion to the total dispersion):

$$r = \frac{\frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{var_x * var_y}}$$

Correlation: Exercise & R Commands

Exercise:

- Is there an association between the evaluation of music and presentation?
- Is there an association between the evaluation of comedy and competitions?



| • | station | | Variables |
|---|---|---|--|
| • | station_cluster | | |
| | station_cluster service informative_news entertaining_news current_music old_music activating_music relaxing_music informative_presentation entertaining_presentation pleasant_voice witty_comedy funny_comedy entertaining_competitions | • | news music presentation comedy competitions programme gender |
| • | attractive_prices | • | age |
| | | • | age_groups current_ music_A |

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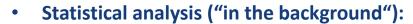
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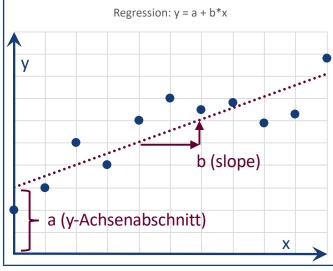
• The linear regression examines the linear effect of a metric variable (simple regression) or multiple metric variables (multiple regression) on a metric variable (dependent variable).

Leading question:

- How strong is the effect of a metric variable (simple regression) or multiple metric variables (multiple regression) on another metric variable?
- Regression model/line (result of an analysis):
 - y = a + b * x
 - y: dependent variable ("effect")
 - x: independent variable ("cause")
 - a: y-intercept
 - b: regression coefficient ("much y increases if x increases by one ")



 The regression analysis determines a line whose squared deviations from the observed values are the least (method of least squares)

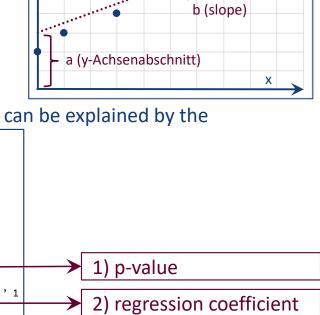


Regression: Brief

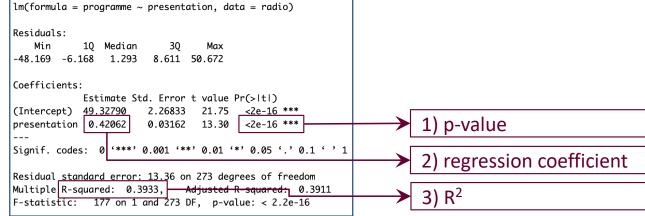
Steps of the analysis:

- Are the p-values < .05 (< .01, < .001)?
 - Does x_i significantly effects y (p-values)?
- How are the regression coefficients (b)?
 - How strong is the effect of x_i on y?
- What is the value for R² (coefficient of determination)?
 - What is the explanatory power of the regression model?
 - R^2 = proportion of the variance of the dependent variable that can be explained by the

independent variables



Regression: y = a + b*x

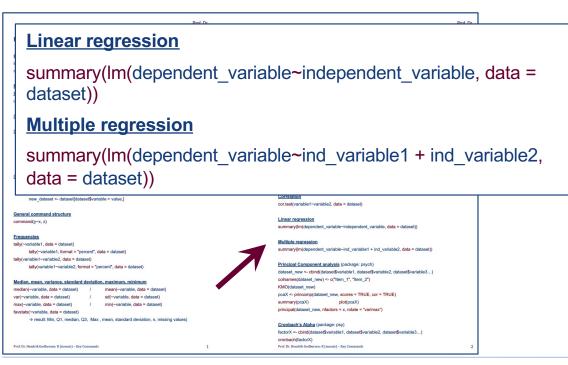


current music A

Regression: Exercise & R Commands

Exercise:

- Which effect does music have on the overall programme?
- Which effect does comedy have on the overall programme?
- Which effect do the five programme elements have on the overall programme?



station Variables station cluster service informative news entertaining news current music news old music music activating music presentation relaxing music comedy informative presentation competitions entertaining_presentation pleasant voice programme witty comedy funny comedy gender entertaining competitions age attractive prices age_groups

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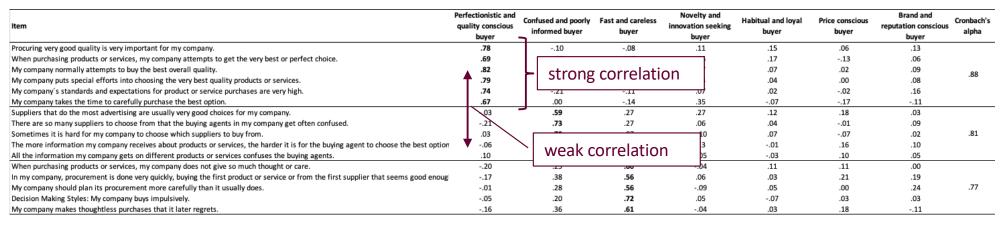
 The principal component analysis is applied to summarise variables/indicators/items on fewer dimensions.

Leading question:

How can multi-dimensional metric variables be allocated to fewer principal components?

Principle idea:

- The items of a component should strongly correlate with each other.
- The items from different components should not or only weakly correlate with each other.



Source: Godbersen, H., Gully, V. (2022): B2B Decision-making Styles Scale. Zusammenstellung sozialwissenschaftlicher Items und Skalen (ZIS).

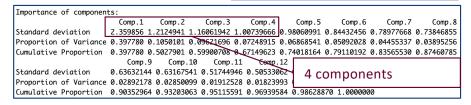
Principal Component Analysis (& Cronbach's α): Brief

- Steps of the analysis
 - 0) Preparation of a new dataset
 - Test if a principal component analysis should be conducted through KMO (Kaiser-Meyer-Olkin test determines the proportion of shared variance among the variables)
 - Determining the number of components through eigenvalues
 - Criterion: components with eigenvalues > 1
 - 3) Determining the loadings (correlation of an item with a component) & allocation of items to components:
 - Precondition: loading > .5
 - Decision: allocation of an item to a component according to the highest loading
 - 4) Interpretation (naming) of components
 - Determining the reliability/one-dimensionality of each of the components through Cronbach's alpha (average inter-item correlation)

Kaiser-Meyer-Olkin factor adequacy Call: KMO(r = pca_radio_data) Overall MSA = 0.85

KMO – accepted values:

- 0.00 to 0.49 unacceptable
- 0.50 to 0.59 miserable
- **0.60** to 0.69 mediocre
- 0.70 to 0.79 middling
- 0.80 to 0.89 meritorious
- 0.90 to 1.00 marvellous



Principal Components Analysis Allocation of items Call: principal(r = pca_radio_data, nfactors = Standardized loadings (pattern matrix) based upon correlation matrix RC4 RC3 RC2 h2 service 0.16 0.78 | 0.18 -0.10 0.67 0.33 1.2 0.12 | 0.90 | 0.03 | 0.02 | 0.83 | 0.17 | 1.0 informative_news 0.48 0.47 0.04 0.35 0.58 0.42 2.8 Entertaining_new 0.19 -0.02 -0.02 0.77 0.62 0 38 1 1 current_music old music \$sample.size Γ17 275

Cronbach's α – accepted values:

- > **0.6** ("hard" criterion)
- > **0.7** ("soft" criterion)

2 0 38 1 1
> cronbach(comp_entertainment)
\$ sample.size
[1] 275

\$ number.of.items
[1] 5

\$ alpha
[1] 0.8511712

Principal Component Analysis (& Cronbach's α): Exercise & R Commands

Exercise:

- Which components can be formed from the programme attributes?
 ("How can the programme attributes be be combined to form new variables?")
- Evaluate the reliability (one-dimensionality) of the new components?

```
Principal Component analysis (package: psych)

dataset_new <- cbind(dataset$variable1, dataset$variable2...)

colnames(dataset_new) <- c("Item_1", "Item_2")

KMO(dataset_new)

pcaX <- princomp(dataset_new, scores = TRUE, cor = TRUE)

summary(pcaX)

plot(pcaX)

principal(dataset_new, nfactors = x, rotate = "varimax")

Cronbach's Alpha (package: psy)

factorX <- cbind(dataset$variable1, dataset$variable2...)

cronbach(factorX)
```

| • | station | | Variables |
|---|---------------------------|---|------------------|
| • | station_cluster | | |
| | | | |
| • | service | | |
| • | informative_news | | |
| • | entertaining_news | | |
| • | current_music | | |
| • | old_music | • | news |
| • | activating_music | • | music |
| • | relaxing_music | • | presentation |
| • | informative_presentation | • | comedy |
| • | entertaining_presentation | • | competitions |
| • | pleasant_voice | | |
| • | witty_comedy | • | programme |
| • | funny_comedy | | |
| • | entertaining_competitions | • | gender |
| • | attractive_prices | • | age |
| | | | |
| | | • | age_groups |
| | | • | current_ music_A |
| | | | |

Prof. Dr. Hendrik Godbersen